

Objective: *To discover patterns in graphing trigonometric functions.*

Review:

When provided with an absolute value function written in standard form ($y = a|x - h| + k$), we can create a graph by identifying the transformations. List the transformations for each of the following:

a.) $y = 2|x - 4| + 3$

b.) $y = |x + 5| - 1$

c.) $y = -|x - 1| + 6$

d.) $y = -\frac{1}{2}|x + 2| - 2$

Predict:

Using the same process, predict how the sine function ($y = a \sin(bx - c) + d$) is transformed below:

a.) $y = 2 \sin(x - 4) + 3$

b.) $y = \sin(x + 5) - 1$

c.) $y = -\sin(x - 1) + 6$

d.) $y = -\frac{1}{2} \sin(x + 2) - 2$

Explore:

We will now explore these transformations further. Go to student.desmos.com and enter in the class code **772GVW**. Follow all of the prompts on the screen.

Slides 1 and 2: In your own words, determine what the various parts of the equation do by using the sliders. When given a sine function in the form $y = a \sin(bx - c) + d$ or a cosine function in the form $y = a \cos(bx - c) + d$

a changes

b changes

c changes

d changes

Vocabulary:

Phase Shift: The number of units the graph has been shifted in the horizontal direction from its usual position

Amplitude: The height of the function from its midline

Vertical Shift: The number of units the graph has been shifted in the vertical direction from its usual position

Period: The shortest repeating portion of the graph is called a cycle and the horizontal length of each cycle is called the period.

Slide 3: Changing the value of a best describes the:

- | | |
|-------------------|--------------|
| A. Phase Shift | B. Amplitude |
| C. Vertical Shift | D. Period |

Slide 6: Changing the value of b best describes the:

- | | |
|-------------------|--------------|
| A. Phase Shift | B. Amplitude |
| C. Vertical Shift | D. Period |

Slide 9: Changing the value of c best describes the:

- | | |
|-------------------|--------------|
| A. Phase Shift | B. Amplitude |
| C. Vertical Shift | D. Period |

Slide 12: Changing the value of d best describes the:

- | | |
|-------------------|--------------|
| A. Phase Shift | B. Amplitude |
| C. Vertical Shift | D. Period |

Extension: Navigate to <https://www.desmos.com/calculator/rusqxyr4ux>. Make your graph match the sound wave, as instructed on Desmos. Record the values that made your graph match the sound wave below:

$a =$

$b =$

$c =$

$d =$

Reflect:

1. Write an equation for a sine graph that has an amplitude of 2.
2. Write an equation for a cosine graph that has been vertically shifted.
3. Provide the equations for two sine graphs that have the same period.