

**Objective:** to solve simultaneous functions using the graphing calculator.

**Warm-up:**

1. Factor  $x^2 - 6x + 5$

$(x-1)(x-5)$

	$x$	$-5$
$x$	$x^2$	$-5x$
$-1$	$-x$	$5$

2. Factor  $(x^3 - 2x^2) - 3x + 6$

$x^2(x-2) - 3(x-2)$

$\Rightarrow (x^2-3)(x-2)$

3. Solve  $(x^2 - 1)(x^2 - 2x + 1) = 0$

$(x-1)(x+1)(x-1)(x-1) = 0$

$\downarrow$        $\downarrow$        $\downarrow$        $\downarrow$   
 $x=1$      $x=-1$      $x=1$      $x=1$

$(-1, 0), (1, 0)$

4. What does a solution to an equation tell you?

It tells you where the x-intercepts are located!

**Steps to solving using a graphing calculator:**

1. Type the left side of the equation into the graphing calculator ( $Y_1$ )
2. Type the right side of the equation into the graphing calculator ( $Y_2$ )  
**Note:** Be sure to put parenthesis around both the numerator & denominator for fractions.
3. Graph the equations
4. 2<sup>nd</sup> → Calc → Intersect.... Then follow the prompts to give the calculator a restricted domain.

**Example 1:** Solve each of the following using your graphing calculator (round to the nearest thousandth).

a.  $\sqrt{x+5} = 5 - \sqrt{x}$

$Y_1 = \sqrt{x+5}$

$Y_2 = 5 - \sqrt{x}$

$x = 4$

b.  $\frac{3x+5}{x-2} = \frac{x-6}{5x+1}$

$Y_1 = (3x+5)/(x-2)$

$Y_2 = (x-6)/(5x+1)$

$x = -2.75, 0.18$

c.  $\frac{1}{2}x^2 - 5 = -x + 3$

$Y_1 = (1/2)x^2 - 5$

$Y_2 = -x + 3$

$x = -5.12, 3.12$

d.  $\log(x+7) = |2x+5| - 3$

$Y_1 = \log(x+7)$

$Y_2 = |2x+5| - 3$

$x = -4.22, -0.60$

e.  $\sqrt{3x+2} = \sqrt{6x+4}$  \*no calculator needed!

$$\begin{array}{r} 3x+2 = 6x+4 \\ -3x \quad -3x \\ \hline 2 = 3x+4 \\ -4 \quad -4 \\ \hline \end{array}$$

$$\frac{-2}{3} = \frac{3x}{3}$$

$$x = -2/3$$

g.  $-\frac{1}{4}|3x-5| = 2 \log(3-x)$

$$y_1 = -(1/4)|3x-5|$$

$$y_2 = 2 \log(3-x)$$

$$x = 2.52$$

f.  $3^{x+5} = 3 \ln(x+6) + 2$

$$y_1 = 3^{(x+5)}$$

$$y_2 = 3 \ln(x+6) + 2$$

$$x = -5.36, -3.61$$

h.  $\sqrt{3x-2} = 4 - \sqrt{2x-3}$

$$y_1 = \sqrt{3x-2}$$

$$y_2 = 4 - \sqrt{2x-3}$$

$$x = 2.68$$

**Reflect:** What are the key steps to remember from today?

**Practice:** Solve each of the following using your graphing calculator (round to the nearest thousandth).

a.  $x^3 = x^2 - 1$

$$y_1 = x^3$$

$$y_2 = x^2 - 1$$

$$x = -.755$$

b.  $\sqrt{3x-2} = 4 - \sqrt{2x-3}$

$$y_1 = \sqrt{3x-2}$$

$$y_2 = 4 - \sqrt{2x-3}$$

$$x = 2.685$$

c.  $3^{x+5} = 3 \ln(x+6) + 2$

$$y_1 = 3^{(x+5)}$$

$$y_2 = 3 \ln(x+6) + 2$$

$$x = -5.357, -3.608$$

d.  $-\frac{1}{4}|3x-5| = 2 \log(3-x)$

$$y_1 = -(1/4)|3x-5|$$

$$y_2 = 2 \log(3-x)$$

$$x = 2.522$$

e.  $\frac{1}{2}x^2 - 5 = -x - 1$

$$y_1 = (1/2)x^2 - 5$$

$$y_2 = -x - 1$$

$$x = -4, 2$$

f.  $\sqrt{3x+2} = \sqrt{6x+4}$

$$\begin{array}{r} 3x+2 = 6x+4 \\ -3x \quad -3x \\ \hline \end{array}$$

$$\begin{array}{r} 2 = 3x+4 \\ -4 \quad -4 \\ \hline \end{array}$$

$$\frac{-2}{3} = \frac{3x}{3}$$

$$x = -2/3$$