

Part I Objective: To simplify and multiply rational expressions

Warm Up:

1. Factor the following expressions.

a. $x^2 + 3x - 4$

b. $4x^2 - 9$

c. $6x^2 + x$

2. Simplify the following expressions.

a. $x^3x^2 =$

b. $\frac{x^5}{x^2} =$

Vocabulary:

Simplified Form: A rational expression that has no common factors in the numerator and denominator.

Extraneous Solution: A solution of a simplified version of the equation that does not satisfy the original equation.

Excluded Value: The value of a variable that will make the denominator equal to zero.

Example 1: Simplify the expression and identify the excluded values.

a. $\frac{x^2+5x}{x^2}$

b. $\frac{6x+24}{x^2+7x+12}$

Example 2: Multiply, simplify, and identify the excluded values.

a. $\frac{5x-15}{4x^2} \cdot \frac{x^3}{6x-18}$

b. $\frac{4xy^3}{x^2y} \cdot \frac{y}{8x}$

c. $\frac{6x-12}{x^2-9x+18} \cdot \frac{7x-21}{5x-10}$

d. $\frac{2x^2-2}{x^2-6x-7} \cdot (x^2 - 10x + 21)$

Part II Objective: To divide rational expressions

Dividing Fractions

*****Dividing by a fraction is the same as multiplying by its reciprocal*****

Division Rule: $\frac{a}{b} \div \frac{c}{d} = \frac{a}{b} \cdot \frac{d}{c}$

Example 3: Divide, simplify, and identify the excluded values.

a. $\frac{5x}{3x-12} \div \frac{x^2-2x}{x^2-6x+8}$

b. $\frac{3}{x-8} \div \frac{x^2+3x}{x^2+x-6}$

c. $\frac{x^2+5x-24}{2x+2} \div \frac{3x+24}{x^2-8x-9}$