



Integrated Math III

Final Exam Review Packet

Semester 1 – 2019

Name _____

Semester 1 Formulas

ALL formulas below will be given within appropriate questions on the final exam

Formulas:	$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$
Area of a Triangle: $A = \frac{1}{2} \cdot b \cdot h$	Area of a Rectangle/Square: $A = b \cdot h$
Area of a Parallelogram: $A = b \cdot h$	Area of a Rhombus: $A = b \cdot h$ or $A = \frac{1}{2} \cdot d_1 \cdot d_2$
Area of a Kite: $A = \frac{1}{2} \cdot d_1 \cdot d_2$	Area of a Trapezoid: $A = \frac{1}{2} \cdot h(b_1 + b_2)$
$(x-h)^2 + (y-k)^2 = r^2$	$(x-h)^2 = 4p(y-k)$ $(y-k)^2 = 4p(x-h)$

Formulas:	Prism	V = Bh	Cone	$V = \frac{1}{3}\pi r^2 h$	$SA = \pi r^2 + \pi r l$
	Cylinder	$V = \pi r^2 h$	Sphere	$V = \frac{4}{3}\pi r^3$	$SA = 4\pi r^2$
	Pyramid	$V = \frac{1}{3}Bh$			
:					

Use the space below to list any other formulas you might need (that will not be given to you).

Unit 1: Analytical Geometry

- 1. For a circle with center (5, -2) and a point at (-3, 8) ...
 - a. Determine the radius.

b. Write the equation of the circle.

2. Given the line $y = \frac{4}{3}x - 5$, write the equation of a line perpendicular to the given line that goes through the point (6, -1) in point-slope form.

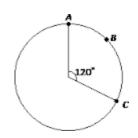
3. Given the line $y = \frac{4}{3}x - 5$, write the equation of a line parallel to the given line that goes through the point (6, -1) in slope-intercept form.

- 4. Given the equation of a circle is $x^2 + y^2 8x + 6y + 16 = 0$, find each of the following:
 - a. The equation in standard form

- b. The center c. The radius
- d. The area c. The diameter
- d. The circumference of the circle
- e. Justify if (-3, 5) is on the circle

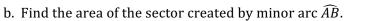
	↑ y
5. Given the equation of the parabola: $(x + 2)^2 = 8(y + 2)$, provide the missing	· · · · · · · · · · · · · · · · · · ·
	· · · · · · · · · · · · · · · · · · ·
information, then graph.	61
	\downarrow
a Vortov	· · · · · · · · · · · · · · · · · · ·
a. Vertex	· · · · · · · · · · · · · · · · · · ·
×	
· · · · · · · · · · · · · · · · · · ·	-10 - 8 - 6 - 4 - 2 - 7 - 7 - 4 - 6 - 8 - 10 r
b. P-value	-10 -8 -6 -4 -2 = 2 -2 -2 -4 -6 -8 -10 x
	· · · · · · · · · · · · · · · · · · ·
	· · · · · · · · · · · · · · · · · · ·
c. Focus	-6
c. Focus	· · · · · · · · · · · · · · · · · · ·
d. Directrix	
	\checkmark
	•
	1 y
6. Given the equation of the parabola: $(y + 1)^2 = -12(x - 3)$, provide the missing	
	· · · · · · · · · · · · · · · · · · ·
information, then graph.	$ \cdot \cdot$
, o i	
a. Vertex	· · · · · · · · · · · · · · · · · · ·
	· · · · · · · · · · · · · · · · · · ·
	$2 \downarrow 2 \downarrow$
b. P-value	$\leftarrow + + + + + + + + + + + + + + + + + + +$
	-10 - 8 - 6 - 4 - 2 $2 - 4 - 6 - 8 - 10 x$
	· · · · · · · · · · · · · · · · · · ·
c. Focus	
	· · · · · · · · · · · · · · · · · · ·
d. Directrix	\cdots
	· · · · · · · · · · · · · · · · · · ·
4	\downarrow

- 7. Using the sector below with a radius of 5 cm.
 - a. Find the length of the minor arc \widehat{AC} .

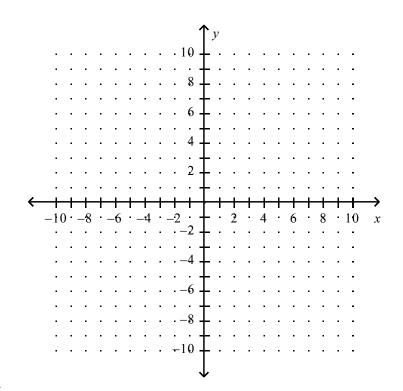


b. Find the area of the sector created by minor arc \widehat{AC} .

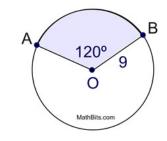
- 8. Using the sector below with a radius of 9 cm.
 - a. Find the length of the minor arc \widehat{AB} .



- 9. Jose owns a plot of land in the shape of a quadrilateral. If the outside of this plot of land has endpoints of *A*: (−3, 5), *B*: (4, 5), *C*: (2, −2), and *D*: (−5, −2).
 - a. Classify quadrilateral ABCD. Justify your reasoning using slope and distance.



- b. Find the perimeter.
- c. Determine the area.



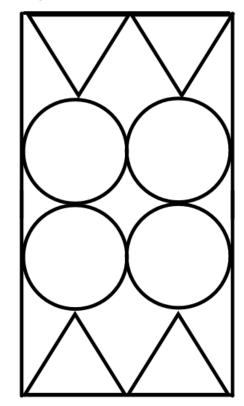
Unit 2: Geometric Proofs and Modeling

10. What are the cross sections formed by each of the following shapes?

a. Cylinder	b. Cone	c. Sphere:
Vertical:	Vertical:	Vertical:
Horizontal:	Horizontal:	Horizontal:

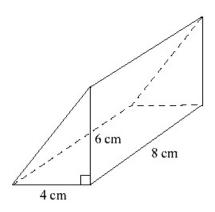
11. Determine which 3-dimensional shape is formed by each of the following.

- a. A rectangle rotated around a segment
- b. A right triangle rotated around a segment
- c. A circle rotated along its diameter
- 12. I purchased an area rug that measures 24" by 48". The design within the rug contained 4 circles with radius of 6" and 4 equilateral triangles with lengths of 12". Find each of the following: (not drawn to scale)
 - a. Area of one triangle
 - b. Area of one circle
 - c. Total area of rug
 - d. Total area of all triangles and circles



e. Area of the rug not containing triangles or circles.

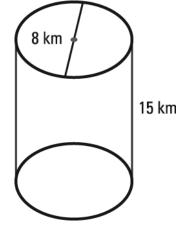
- 13. Use the triangular prism to calculate:
 - a. Total Surface Area



b. Volume

14. Use the diagram to calculate:

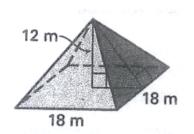
a. Total Surface Area



b. Volume

15. Use the square pyramid to calculate:

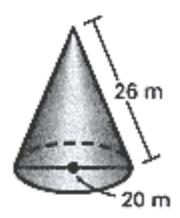
a. Total Surface Area



b. Volume

16. Use the cone to calculate:

a. Total Surface Area



b. Volume

17. A sphere with a radius of 10.

a. Total Surface Area

b. Volume

18. The average television has a mass of 12,473.79 grams. Find the density if the volume of an average television is 1,507.92 cubic inches.

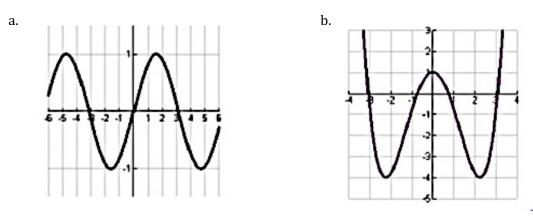
 The population density of Wrap, IL is 4,564 people per square mile. How many people live in Wrap if the town covers 9.71 mi²

20. The population density of Hot Dog, IL is 5,155 people per square mile. If there are 16,887 people living outside the bun, how many square miles is Hot Dog, IL?

Unit 3: Representing Functions

21. Use the graph to identify the following:	100 (-2,44) 50
Relative minimum(s):	
Relative maximum(s):	$\begin{array}{cccccccccccccccccccccccccccccccccccc$
Absolute maximum(s):	- 150 -
Absolute minimum(s):	-200 _
Increasing interval(s):	
Decreasing interval(s):	
Domain:	Range:
X-Intercept(s):	Y- Intercept(s):

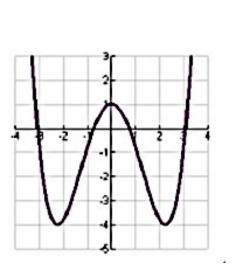
22. Use the graphs below to identify the type of symmetry. Draw the line or point where the graph is symmetric.



23. Given the functions $f(x) = x^2$ and $g(x) = -3(x + 1)^2 + 4$, determine how each number transforms the new graph **(be specific)**.



24. Use the graph below to identify the indicated key features.

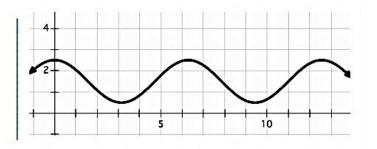


Type of symmetry: Relative maximum(s): Relative minimum(s): Absolute maximum(s): Absolute minimum(s): Intervals of increasing: Intervals of decreasing: End behavior: $As x \rightarrow \infty, f(x) \rightarrow As x \rightarrow -\infty, f(x) \rightarrow As x \rightarrow -\infty, f(x) \rightarrow As x \rightarrow -\infty, f(x) \rightarrow Compared by the second second$

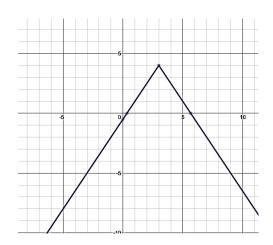
X-Intercept(s):

Y-Intercept(s):

25. Using the following graph, determine if it demonstrates periodicity. If so, what is the period?

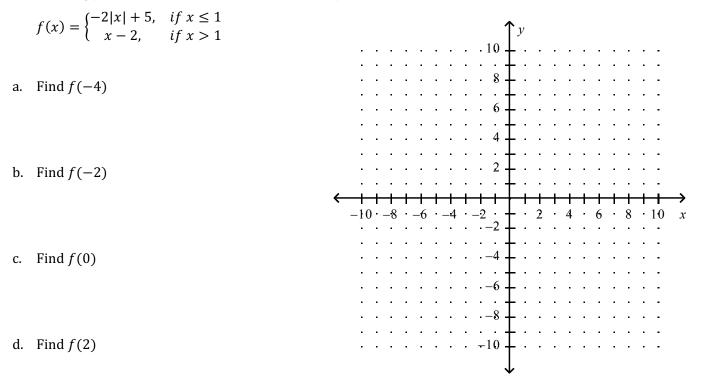


- 26. Use the graph to answer the questions below.
 - a. Describe the transformations from the parent graph to the provided one.



b. Write the equation for this graph.

27. Graph the following piecewise function. Then, answer the questions that follow.



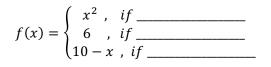
e. Find f(4)

28. Graph the following piecewise function. Then, answer the questions that follow.

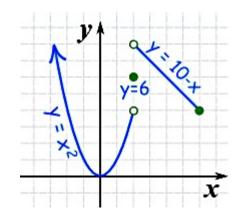
$$f(x) = \begin{cases} 2x + 5, & \text{if } x \le -2 \\ -4, & \text{if } -2 < x < 3 \\ \frac{2}{3}x - 2, & \text{if } x \ge 3 \end{cases}$$

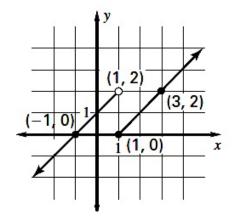
- e. Find f(3)
- f. Find f(6)

29. Write a piecewise function for the following graph:



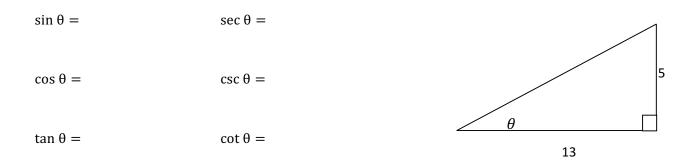
30. Write a piecewise function for the following graph:





Unit 4: Trigonometric Representations & Modeling

31. Give the EXACT value for the six trigonometric values of θ .

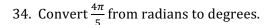


32. Given that
$$\theta$$
 lies in quadrant IV and $\cos \theta = \frac{5}{13}$, find...

a. $\sin \theta$

b. $tan \theta$

33. Convert 130° from degrees to radians.



Find the reference angle in degrees _____

Find a positive coterminal angle in degrees: _____

Find a negative coterminal angle in degrees: _____

Find the reference angle in degrees _____

Find a positive coterminal angle in degrees: _____

Find a negative coterminal angle in degrees: _____

35. Find the EXACT value (no decimals) of cos 240°.

37. Find the exact value (no calculator) for the following trig functions if $\cot = -\frac{20}{21}$ and the terminal side is in quadrant IV.

 $\sin \theta = ___$ $\cos \theta = ___$ $\tan \theta = ___$

38. Given an angle with measure 150°...

a. Sketch the angle in standard position.

b. Determine the quadrant the terminal side lies in. _____

c. Find the measure of the reference angle. _____

d. Draw a reference triangle & evaluate all 6 trig functions.

$\sin 150^{\circ} = $	$\cos 150^\circ = $	tan 150° =
csc 150° =	sec 150° =	cot 150° =

39. Simplify: $\sin^2 \theta - 3 + \cos^2 \theta$ 40. Verify: $\sin \theta \cot \theta = \cos \theta$

- 41. As I prepared to come home from Charleston, SC, my family waited for me at the airport. They noticed that my plane was 21,000 feet above the ground, the angle of elevation was 13°.
 - a. How far was I still away from my family?

b. What is the horizontal distance that I was from the airport?

Unit 5: Graphing and Modeling Trigonometric Equations

42. What is the period of the graph represented by the equations below?

a.
$$f(x) = \cos(4x)$$

b. $f(x) = 3\sin(\frac{1}{2}x)$
c. $f(x) = 4\cos(x)$

43. What is the amplitude of graph represented by the equations below?

a.
$$f(x) = 4\sin(3x) + 5$$

b. $f(x) = \cos(x) - 1$
c. $f(x) = -3\sin 4x$

44. What is the horizontal shift of the equation $y = -2\cos(x + \pi) - 1$? 45. What is the vertical shift of the equation $y = 2\sin(x - \pi) + 3$?

46. Given the function $y = 2\sin(x) - 3$, fill in the following blanks and graph:

47. Given the function $y = -\cos(2x)$, fill in the following blanks and graph:

n the function = $2 \sin\left(\frac{1}{2}x\right) + 1$, fill in the following blanks and graph: Phase/Horizontal Shift: Range:							
$\frac{1}{2\pi} \cdot \pi = 0$ $\pi = 2 \sin\left(\frac{1}{2}x\right) + 1, \text{ fill in the following blanks and graph:}$ $\frac{1}{2\pi} \cdot \pi = 0$ $\frac{1}{2} x + 1, \text{ fill in the following blanks and graph:}$ $\frac{1}{2\pi} \cdot \pi = 0$	Phase	e/Horizonta	al Shift:		I	Range:	
n the function = $2 \sin\left(\frac{1}{2}x\right) + 1$, fill in the following blanks and graph: $mplitude: Vertical Shift: Period: Phase/Horizontal Shift: Range: \frac{-2\pi}{2\pi} - \frac{\pi}{2\pi} = 0$			6				
n the function = $2 \sin\left(\frac{1}{2}x\right) + 1$, fill in the following blanks and graph: mplitude: Vertical Shift: Period: Phase/Horizontal Shift: Range:			5				
n the function = $2 \sin\left(\frac{1}{2}x\right) + 1$, fill in the following blanks and graph: mplitude: Vertical Shift: Period: Phase/Horizontal Shift: Range:							
n the function = $2 \sin\left(\frac{1}{2}x\right) + 1$, fill in the following blanks and graph: m the function = $2 \sin\left(\frac{1}{2}x\right) + 1$, fill in the following blanks and graph: mplitude: Vertical Shift: Period: Phase/Horizontal Shift: Range:							
n the function = $2 \sin\left(\frac{1}{2}x\right) + 1$, fill in the following blanks and graph: m the function = $2 \sin\left(\frac{1}{2}x\right) + 1$, fill in the following blanks and graph: mplitude: Vertical Shift: Period: Phase/Horizontal Shift: Range:							
n the function = $2 \sin\left(\frac{1}{2}x\right) + 1$, fill in the following blanks and graph: m the function = $2 \sin\left(\frac{1}{2}x\right) + 1$, fill in the following blanks and graph: mplitude: Vertical Shift: Period: Phase/Horizontal Shift: Range:							
n the function = $2 \sin\left(\frac{1}{2}x\right) + 1$, fill in the following blanks and graph: amplitude: Vertical Shift: Period: Phase/Horizontal Shift: Range:	-2π	-π	0	π	2π	3π	41
n the function = $2 \sin\left(\frac{1}{2}x\right) + 1$, fill in the following blanks and graph: amplitude: Vertical Shift: Period: Phase/Horizontal Shift: Range:							
n the function = $2 \sin\left(\frac{1}{2}x\right) + 1$, fill in the following blanks and graph: amplitude: Vertical Shift: Period: Phase/Horizontal Shift: Range:							
n the function = $2 \sin\left(\frac{1}{2}x\right) + 1$, fill in the following blanks and graph: amplitude: Vertical Shift: Period: Phase/Horizontal Shift: Range:							
n the function = $2 \sin\left(\frac{1}{2}x\right) + 1$, fill in the following blanks and graph: amplitude: Vertical Shift: Period: Phase/Horizontal Shift: Range:			-5				
Amplitude: Vertical Shift: Period: Phase/Horizontal Shift: Range:							
Phase/Horizontal Shift: - -					ing blanks an	u graph.	
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	٨						J.
	Amplitude:						d:
			Vert	ical Shift:		Perio	
			Vert	ical Shift:		Perio	
			Vert	ical Shift:		Perio	
			Vert	ical Shift:		Perio	
			Vert	ical Shift:		Perio	
			Vert	ical Shift:		Perio	
			Vert	ical Shift:		Perio	
	Phase	e/Horizonta	Vert	ical Shift:	 I	Period	
	Phase	e/Horizonta	Vert	ical Shift:	 I	Period	
	Phase	e/Horizonta	Vert	ical Shift:	 I	Period	
	Phase	e/Horizonta	Vert	ical Shift:	 I	Period	
	Phase	e/Horizonta	Vert	ical Shift:	 I	Period	

49. Using the graph to the right, identify the:

a. Amplitude

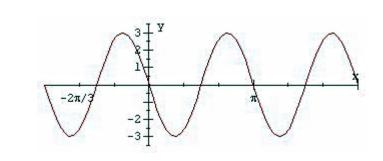
b. Period

c. Horizontal shift

d. Vertical Shift

e. Range

f. Equation



50. A fisherman noticed that the height of a bobber oscillated from 6 to 10 feet every 4 seconds. Identify each of the following

a. Midline

b. Amplitude

c. Period

- d. Equation (express this function in terms of sine)
- 51. Write an equation to best represents the following situations:

a. The time between high tides is 8 hours. The high-tide depth is 12 feet and the low-tide depth is 4 feet.

b. Mrs. Kelleher is pushing her daughter on a swing. When she starts the swing at its highest point, her daughter is 6 feet above the ground. At the lowest point, the swing is 2 feet above the ground. It takes approximately 2 seconds for the swing to leave and come back to Mrs. K.

52. Write the equation that corresponds with each graph below.

